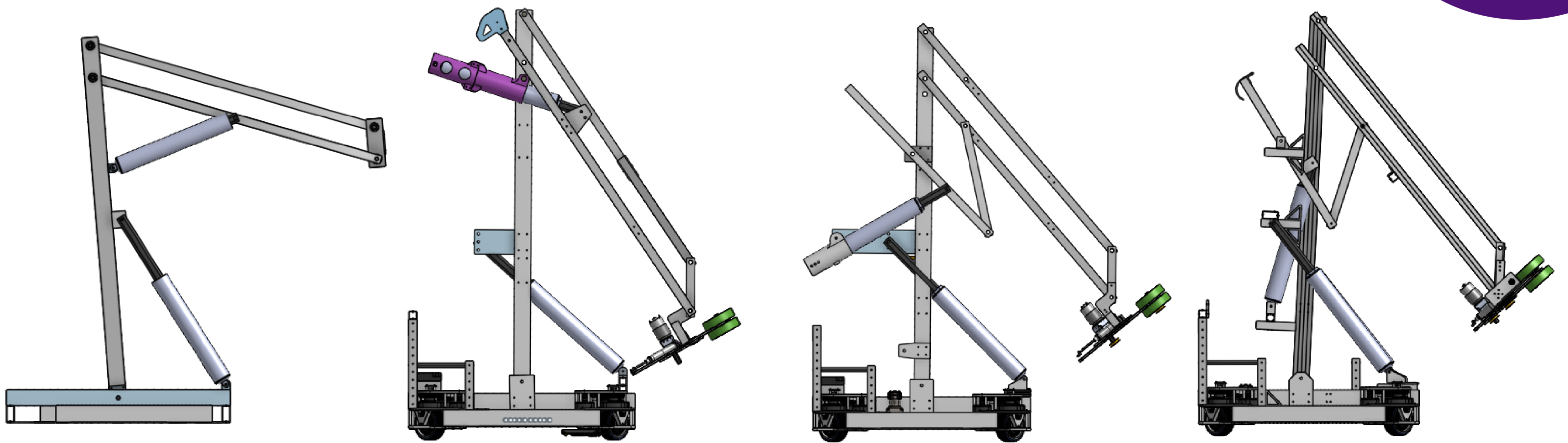
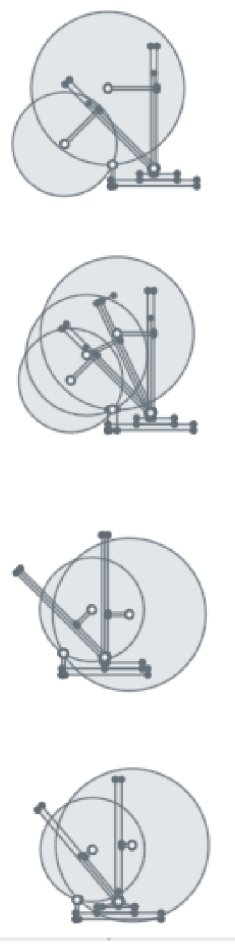


Main Arm Design Evolution

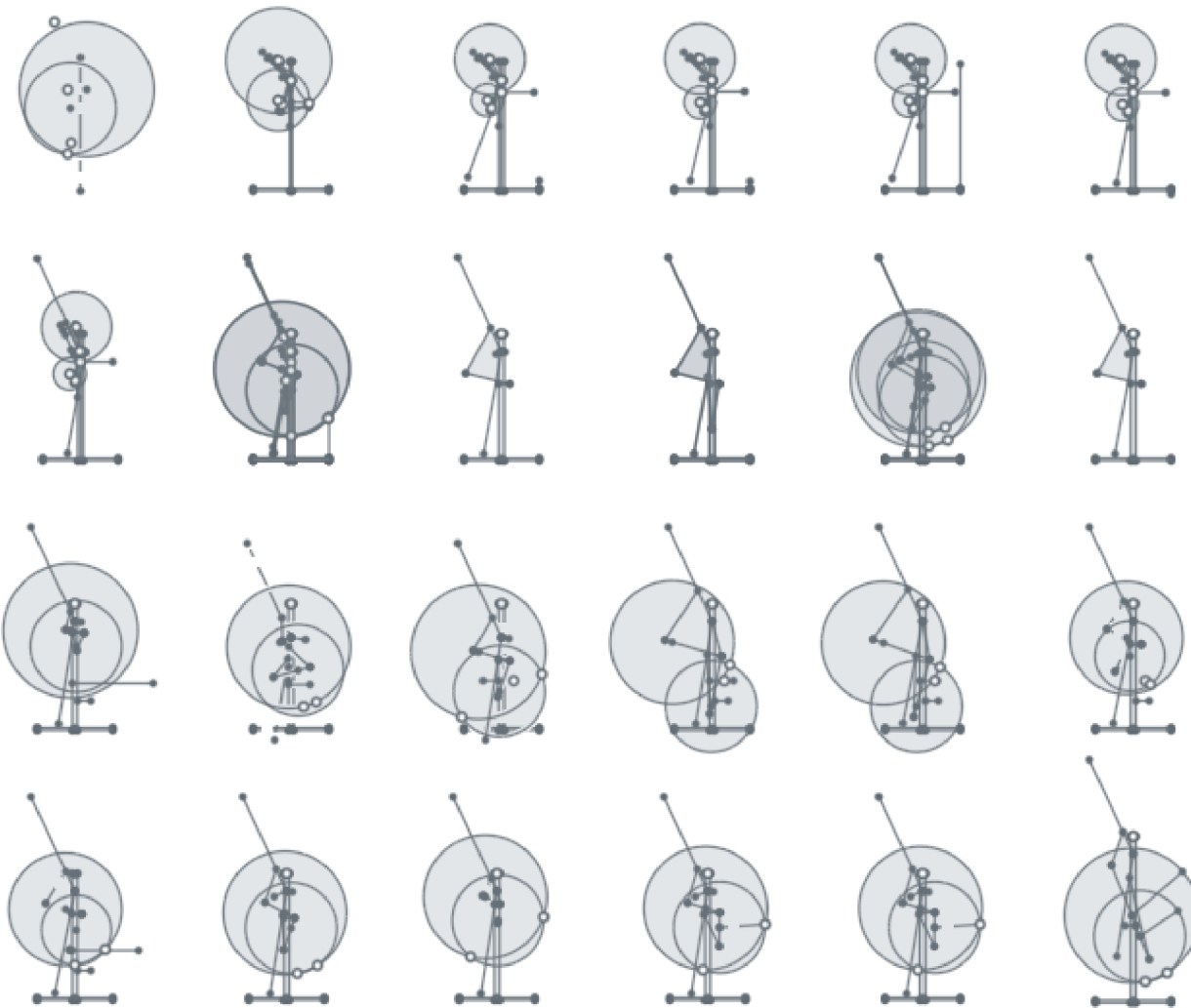


Geometry

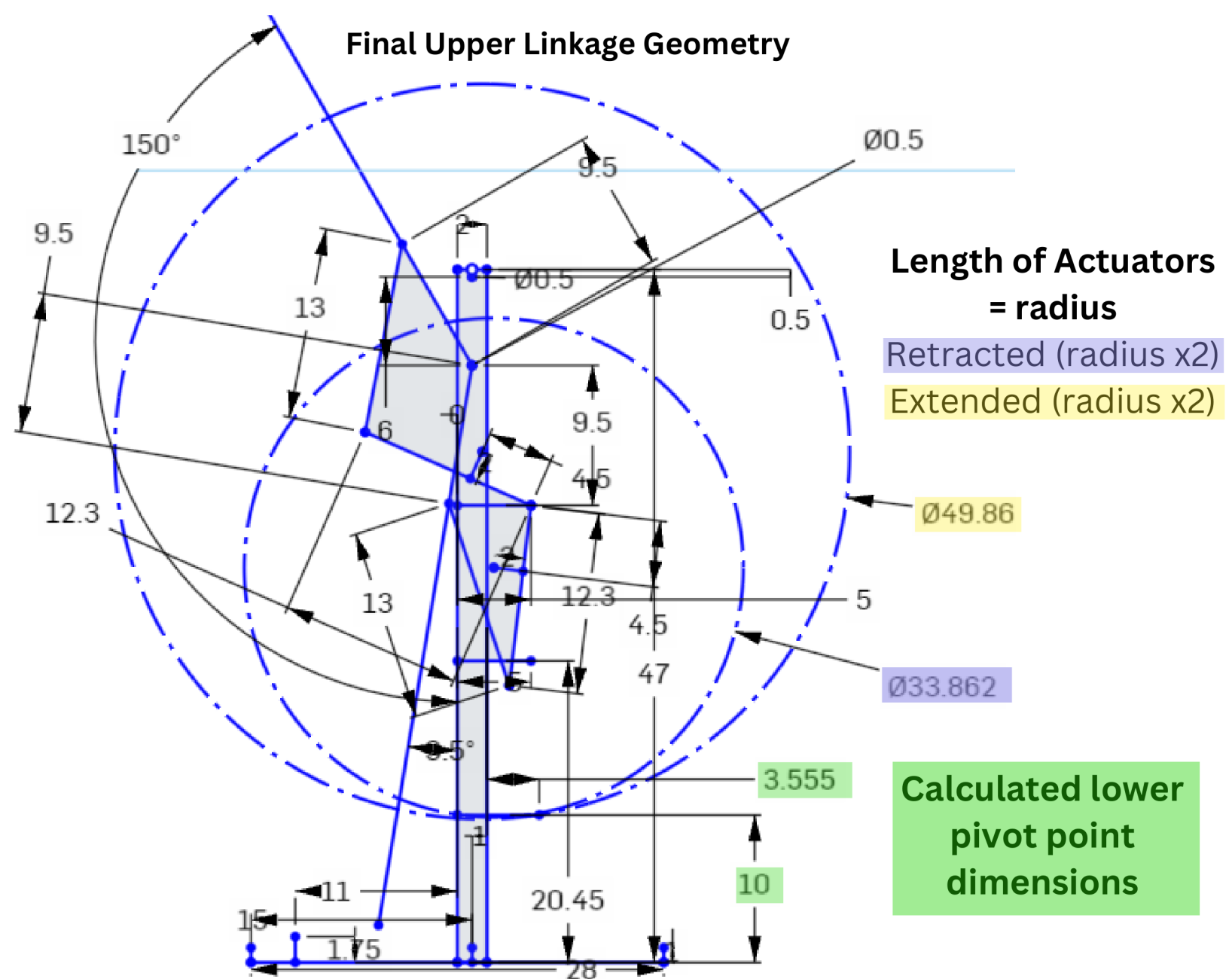
Lower Actuator Geometry Iterations



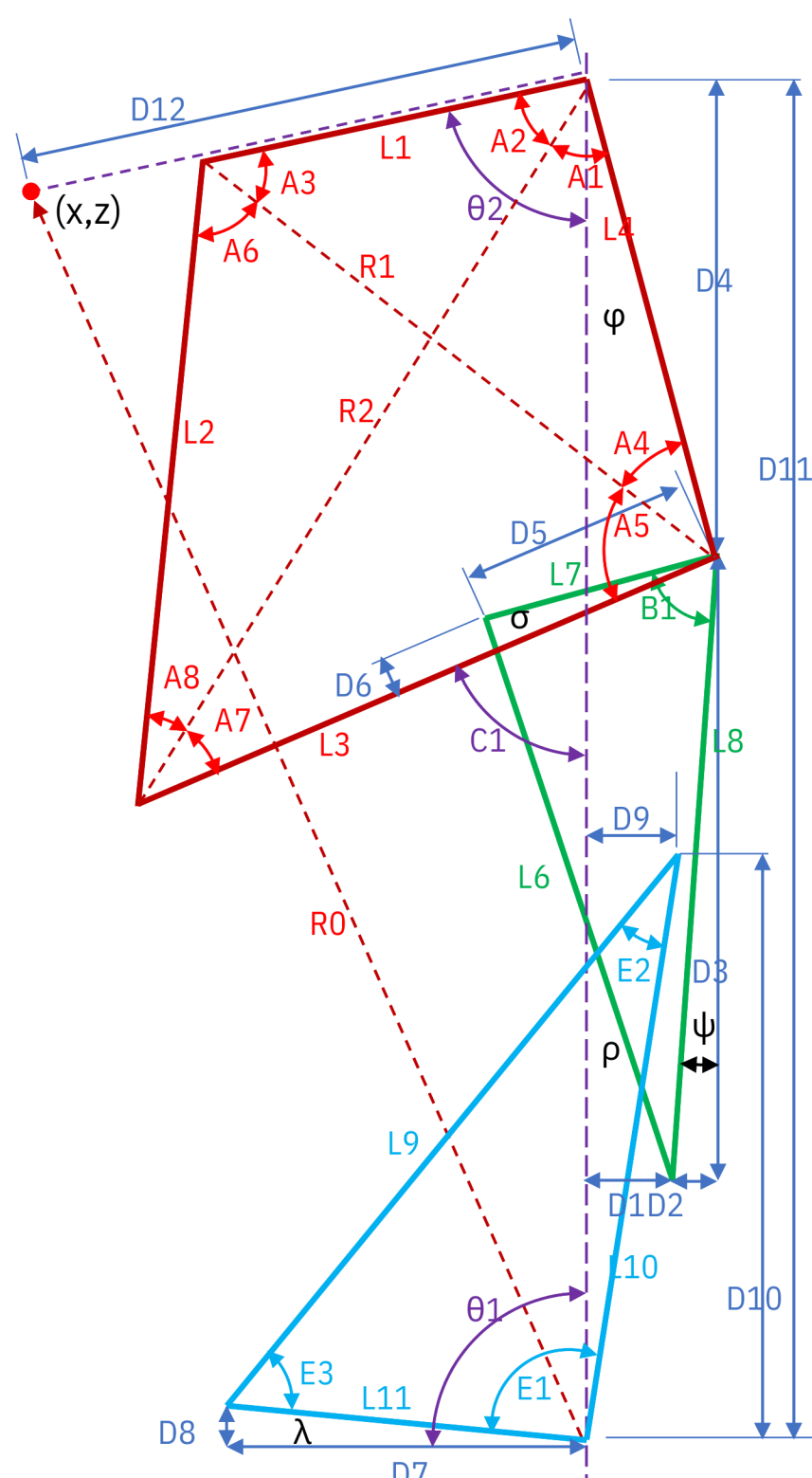
Upper Linkage Geometry Iterations



Final Upper Linkage Geometry



Forward and Inverse Kinematics



(Finding L6 and L9, given theta1 and theta2)

Upper Section Steps:

$$\begin{aligned} \phi &= \text{atan2}(D1+D2, D4) \\ A1+A2 &= \theta2 + \phi \\ R1 &= \sqrt{L1^2 + L2^2 - 2*L1*L2*\cos(A1+A2)} \\ A4 &= \text{asin}(L1*\sin(A1+A2)/R1) \\ A5 &= \pm\text{acos}[(L2+R2-L2122)/(2*L1*R2)] \end{aligned}$$

Middle Section Steps:

$$\begin{aligned} \sigma &= \text{atan2}(D6, D5) \\ \Psi &= \text{atan2}(D2, D3) \\ C1 &= 180^\circ - \phi - A4 - A5, B1 = C1 - \Psi + \sigma \\ B1 &= 180^\circ - A4 - A5 - \phi - \Psi + \sigma \\ L6 &= \sqrt{L2 + L278 - 2*L7*L8*\cos(B1)} \end{aligned}$$

Lower Section Steps:

$$\begin{aligned} \lambda &= \text{atan2}(D8, D7) \\ \rho &= \text{atan2}(D9, D10) \\ E1 &= \theta1 + \rho - \lambda \\ L9 &= \sqrt{L210 + L11^2 - 2*L10*L11*\cos(E1)} \end{aligned}$$

(Finding theta1 and theta2 given L6 and L9)

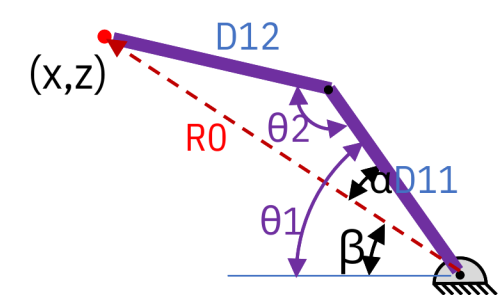
$$\begin{aligned} R2 &= \sqrt{L223 + L4 - 2*L3*L4*\cos(A4+A5)} \\ A1 &= \pm\text{acos}[(L2+R2-L2423)/(2*L4*R2)] \\ A2 &= \pm\text{acos}[(L2+R2-L2122)/(2*L1*R2)] \\ \theta2 &= A1 + A2 - \phi \end{aligned}$$

$$\begin{aligned} B1 &= \pm\text{acos}[(L227 + L8 - \rho^2)/(2*L7*L8)] \\ L C1 &= B1 + \Psi - \sigma \\ A4+A5 &= 180^\circ - \phi - C1 \end{aligned}$$

$$\begin{aligned} E1 &= \pm\text{acos}[(L10^2 + L11^2 - L9^2)/(2*L10*L11)] \\ \theta1 &= E1 - \rho + \lambda \end{aligned}$$

Notes:

- D1, D2, D3, D4, D5, D6, D7, D8, D9, D10, D11, and D12 from
- CAD theta1, theta2 from Inverse Kinematics or L6, L9 from actuator inputs



Inverse Kinematics

$$\begin{aligned} R22 + z20 &= x \\ \theta2 &= \pm\text{acos}[(D2 + D2 - R2 - 11120)/(2*D11*D12)] \\ \beta &= \text{atan2}(z, x) \\ \alpha &= \pm\text{acos}[(D2 + R2 - D2 - 11012)/(2*D11*R0)] \\ \theta1 &= \alpha + \beta \end{aligned}$$

Forward Kinematics

$$\begin{aligned} x &= D11*\cos(\theta1) + D12*\cos(\theta1 - 180^\circ + \theta2) \\ z &= D11*\sin(\theta1) + D12*\sin(\theta1 - 180^\circ + \theta2) \end{aligned}$$

